Object-Oriented Style

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ABSTRACT

Writing programs in continuation-passing style is a good tool for understanding reified continuations and `call/cc`. Similarly, writing programs in an object-oriented style is a good tool for understanding object-oriented language features, such as super (or object) method invocation. We present an object-oriented style and a simple example of its use. From this example, we present protocols that make this style more natural. We then enforce the style and protocols by introducing a macro per class. These macros are macro-generating macros that package the syntactic redundancy of the style, approximating a compiler for a conventional object-oriented language. Exercises are scattered throughout to help the energetic reader develop a deeper understanding of the paper's concepts.

1. INTRODUCTION

We use *style* to mean an encoding of a language idiom generally in some other language. Furthermore, we expect that the style makes explicit everything that matters. One of the advantages of well-defined programming languages is that built-in idioms are abstracted away. But, this is also one of the disadvantages, especially for those who want to completely understand the language. Also a style has the advantage that since everything is explicit, it is clear exactly how it might be embedded in the encoding language. For example, with Scheme as the encoding language, we claim that any value can be a method, and if that value happens to be a procedure of at least one argument, it can be invoked in object-oriented style.

Our object-oriented style for single inheritance uses a small subset of Scheme [1], with its ability to associate variables to values as our mechanism to define classes and objects. Virtually any system with first-class procedures, lists, and vectors is powerful enough to allow one to write in this style. For updateable fields and methods, we also need updateable vectors.

There are three motivations behind the ideas in this paper. First, we want to remove the confusion by some beginners about what *object method invocation* is and how it differs from *super method invocation*. We believe that knowing exactly how, when, and in what lexical scope method tables are built lessens this confusion. Second, we want to clarify the extent to which both kinds of method invocation are just procedure invocations and therefore can lead to long chains of recursive calls (Section 8.4). This seems to have been ignored by most implementors of object-oriented languages, even though two decades ago Cardelli [2], Cook and Palsberg [3], Kamin [6], and Reddy [8] observed how object-oriented programming is related to recursion. Third, we want to demonstrate a style that does not rely on recursion to model classes and objects. This clarifies why the recursion that does arise must be through a dynamically-scoped variable: `this` (or `self`).

1.1 What makes CPS a style?

The restrictions of CPS can be described by a grammar: calls to non-primitives must be tail calls, which implies that arguments must be simple. The simple terms are `lambda` expressions, variables, constants, and combinations of simple terms using primitive calls. The CPS conversion of `lambda` terms requires adding an extra argument, `k`, the continuation, to each `lambda` parameter list, and each `lambda` body must be CPS'd with respect to `k`. This, in turn, requires that all calls to non-primitives have an extra argument, an expression whose value is a procedure of one argument. That procedure is a continuation. Instead of returning a value from a procedure, a value is "returned" by invoking a continuation.

But a style is more than a grammar. These grammatical rules do not take into consideration that the continuation-passing definition is advisory. For example, it is possible to decide in one context that `member` is primitive (i.e., obviously terminates) and in another context that it must, itself, be rewritten in CPS. One must ask oneself, "Will the expression obviously terminate?" If so, then it is okay to treat the expression as if it were a primitive call. But, what if `member` is passed a circular list and we are relying on it being in CPS for trampolining? Then, it should be treated as a non-primitive call and its definition should be CPS'd. So, CPS is a style with the need for protocols just like the object-oriented style that we discuss here. Hence, the grammar is basically a set of guidelines, where the person who does the manual CPSing of a program gets to use judgment.

1.2 Recursion through `it`

Before we get started, let's look at a familiar way of writing and testing an old chestnut: `even?` and `odd?` for mutual recursion. We implement them without using `letrec` or referring to a free variable within a `lambda` expression.

```
(define e/o-procs
  (vector
    (lambda (it n)
      (if (zero? n) #t
        ((vector-ref it 1) it (- n 1))))
    (lambda (it n)
      (if (zero? n) #f
        ((vector-ref it 0) it (- n 1))))))

> e/o-procs
#(#<iseven> #<isodd>)

> ((vector-ref e/o-procs 0) e/o-procs 5)
#f
```

In the definition of `e/o-procs`, there are neither free variables (only primitives and constants) in the `lambda` expressions nor any explicit recursion. (When meaningful, we display anonymous procedures with names.) We have two procedures in the vector. The procedure in the zeroth position of the vector pulls out a procedure from the first position of the vector, and the procedure in the first position of the vector pulls out a procedure from the zeroth position. In each such call, it passes the procedure vector as an additional first argument.

A procedure that takes such an additional first argument corresponds to a *method*, and a vector of such procedures corresponds to an *object*. What makes object-oriented style more interesting than this simple example is that as each vector is built from another such vector, it is constructed in a reasoned way, but we must wait to see how.

The remainder of the paper is structured as follows. In the next section, we present a variant of the classic point/color point example. In section three, we introduce position environments. In the fourth section, we pick a representation of objects and classes and define nine interface operators. In the fifth section, we present the style informally along with the test program written in our style. In section six, we demonstrate some protocols for giving more intuition about object-oriented style. These include introducing the lexical variable `super`, and removing direct reliance on positions to access methods and fields. Then in the seventh section, we present an innocent-looking transformation that again aids reading but has significant implications for characterizing the next two transformations. Having set the stage, we demonstrate how macros can allow the user to ignore the interface operators and can impose the protocols of object-oriented style to create a version where the positions are determined at macro-expansion time. In the ninth section, we present `new`, which not only creates an object but also invokes the appropriate `init` method. Then, we introduce two macros that remove reliance on quoted symbols. In the final section, we revisit our motivations and make some observations about our approach.

2. THE EXAMPLE

The example assumes some familiarity with object-oriented programming concepts. If this example is not simple to follow, skip this section. Our primary purpose is to characterize the example before we get into the details of our object-oriented style. We use the example of points `<p>`, and color points `<cp>`, but we include a method `diag`, which does a diagonal move, and a method `diag&set`, which does a diagonal move of n followed by setting the color represented by n. We also have stationary color points `<scp>`. One of our goals, inspired by the example from Goldberg and Robson [5] (pages 62–65), is to show a simple example that allows us to clarify the distinction between object method calls and super method calls.

Our example is sugared with macros, however, they do not appear until Section 8. A *shadow*, which is a macro, is what we build before we create its associated class, which is a value as in Smalltalk. A shadow contains the necessary compile-time information to model a class as in C++ or Java. We assume the root shadow `<<o>>` and its associated class `<o>` exist. We use `extend-shadow` to extend a shadow just as we might extend a class. The list of variables mentioned after the super shadow contains the field variables of the class (shadow). They are followed by a list of method definitions. After each shadow is built, we use `create-class` to create its associated class. "Shadows" are unusual, however, the method definitions should seem familiar.

```
(define-syntax <<p>>
  (extend-shadow <<o>> (x y)
    ([init
       (method (x^ y^)
         (set! x x^)
         (set! y y^)
         (init super))]
     [move
       (method (dx dy)
         (set! x (+ x dx))
         (set! y (+ y dy)))]
     [get-loc
       (method ()
         (list x y))]
     [diag
       (method (a)
         (move it a a))])))

(define <p> (create-class <<p>> <o>))

(define-syntax <<cp>>
  (extend-shadow <<p>> (hue)
    ([init
       (method (x^ y^ hue^)
         (set! hue hue^)
         (init super x^ y^))]
     [get-hue
       (method () hue)]
     [diag&set
       (method (a)
         (diag it a)
         (set! hue a))])))

(define <cp> (create-class <<cp>> <p>))
```

```
(define-syntax <<scp>>
  (extend-shadow <<cp>> (y)
    ([init
       (method (x^ y^ hue^)
         (set! y ": Stuck: ")
         (init super x^ y^ hue^))]
     [move
       (method (x^ y^)
         (show-y it))]
     [diag
       (method (a)
         (write hue)
         (diag super a))]
     [show-y
       (method () (display y))])))

(define <scp> (create-class <<scp>> <cp>))
```

The test program below is simple. We build objects of `<p>` and `<scp>` (and `<cp>`). Next we make method calls using `mbv` and `invoke`. We determine that `cp` is an object of class `<p>`, but that `p` is not an object of `<scp>` (or `<cp>`). Section 8 and Section 9 explain these features.

```
(define test
  (lambda (c)
    (let ([p (new <p> 1 2)]
          [cp (new c 18 19 9)])
      (mbv diag&set cp 10)
      (list
        (list
          (invoke <<cp>> get-loc cp)
          (invoke <<cp>> get-hue cp))
        (isa? cp <p>)
        (isa? p c)))))

> (begin (write (test <scp>)) (write (test <cp>)))
9: Stuck: (((18 19) 10) #f #t)(((28 29) 10) #t #f)
```

3. POSITION ENVIRONMENTS

In this section, we introduce position environments; a simple operator `enumerate-env` to make them; an operator `append-env` to combine them; and an operator `trim-env` to remove shadowed variables from them. We also introduce "installing" an environment, an unusual way to determine the value of variables.

We use vectors to represent the data structures of object-oriented style. We eventually want to use variables rather than indices, so we need a representation that associates variables with indices. To do this, we introduce position environments.

A *position environment* is a function whose domain is variables, represented by symbols, and whose range is positions, represented by nonnegative integers, where no position appears more than once. A position environment is *gap-free* if it is empty or it associates some variable to position 0 and contains no gaps. We represent a position environment by a list of variable/position pairs, where the positions are in increasing order. We define the value of a variable with such a representation to be the greatest position associated with the variable. A gap-free environment using these pairs is *pure* if no variable appears more than once. Here is a simple way to make a gap-free environment.

```
(define enumerate-env
  (lambda (vars)
    (let loop ([vars vars] [i 0])
      (cond
        [(null? vars) '()]
        [else
          (cons `(,(car vars) ,i)
            (loop (cdr vars) (+ i 1)))])))))

> (define p '(a b c))
> (define q '(a d c))
> (define penv (enumerate-env p))
> (define qenv (enumerate-env q))
> (define renv '([a 3] [d 5] [c 6]))
> penv
([a 0] [b 1] [c 2])
> qenv
([a 0] [d 1] [c 2])
```

We define `append-env` of a position and a pure environment. It tacks the pure environment onto the position environment, but starts the pure environment at one more than the greatest position of the first argument.

```
(define append-env
  (lambda (e p)
    (cond
      [(null? e) p]
      [else
        (append e
          (let ([m (+ (cadar (last-pair e)) 1)])
            (map (lambda (pr)
                   `(,(car pr) ,(+ (cadr pr) m)))
              p)))])))

> (append-env penv qenv)
([a 0] [b 1] [c 2] [a 3] [d 4] [c 5])
> (append-env renv penv)
([a 3] [d 5] [c 6] [a 7] [b 8] [c 9])
```

We revise `append-env` below, so we do not worry about this definition's efficiency.

We can trim the shadowed variables from an environment represented by a list of pairs, since we only care about the greatest positions of the variables.

```
(define trim-env
  (lambda (e)
    (cond
      [(null? e) '()]
      [(assv (caar e) (cdr e)) (trim-env (cdr e))]
      [else (cons (car e) (trim-env (cdr e)))])))

> (trim-env (append-env penv qenv))
([b 1] [a 3] [d 4] [c 5])
```

We *install* environments to get the value of variables. For example, both expressions below yield the value `(0 1 2)`.

```
> (let ([a 0] [b 1] [c 2])
    (list a b c))
> (eval `(let ,penv (list a b c)))
```

Clearly, installation on some level crosses syntax and semantics. It is best, however, to think of this operation as part of a transformation process.

Similarly, we can install a gap-free environment using `let*`. We use `let*`, since we are only interested in the greatest position of each variable. Thus, `a`'s value is 3 (not 0), and `c`'s value is 5 (not 2). If we wish to use `let`, we must trim the environment before we install it.

```
> (let* ([a 0] [b 1] [c 2] [a 3] [d 4] [c 5])
    (list a b c d))
(3 1 5 4)

> (let ([b 1] [a 3] [d 4] [c 5])
    (list a b c d))
(3 1 5 4)
```

When an environment is gap-free, we may represent it with a simple list of variables. We can redefine `append-env` over gap-free environments and thus represent an environment as a list of variables. The result of `append-env` is also gap-free. Its definition is just `append`.

```
(define append-env append)
> (enumerate-env (append-env p q))
([a 0] [b 1] [c 2] [a 3] [d 4] [c 5])
```

`Exercise 1:` Let e_1 be gap-free and e_2 be pure with both represented by a simple list of variables. Rewrite `(trim-env (enumerate-env (append-env` e_1 e_2`)))` so that, except for some anticipated calls to `memv`, we get a one-pass algorithm $\diamond$

4. CLASSES AND OBJECTS

A *class* is represented as a list[1] of three items: a *field environment*, a *method environment*, and a *method vector*. An *object* is like a class but differs in its first item, a *field vector* the size of the field environment of its associated class. A *method* or *field* is *any* value, but if it is a procedure of at least one argument, then it can be invoked in object-oriented style. The `cdr` of a class or object is its *method table*. A *field table* is the field environment of a class along with a field vector of its associated object. Since the field environment is gap-free and the method environment is pure, we represent each with a simple list of variables. Each environment and its associated vector is the same length, allowing us to associate a variable with each vector element. Our interface operators, described below, treat table content independently of its use, therefore the style, itself, dictates how the two kinds of tables may be different.

[1]We have opted for lists instead of records. We want to build our object-oriented style out of primitive pieces like lists, vectors, and `lambda`.

Next we define the nine interface operators `_fx`, `_mx`, `_mp`, `_mp!`, `_fp`, `_fp!`, `_mteq?`, `_n`, and `_mv`.

4.1 Environment extension operators

We introduce interface operators `_fx`, which extends the field environment of a class, and `_mx`, which extends the method environment of a class.

```
(define (_fx c e) (append-env (car c) e))
(define (_mx c e) (append-env (cadr c) e))
```

4.2 Position-based operators

Each position-based interface operator takes a position as its second argument. To access (or update) a method by position, use `_mp` (or `_mp!`). To access (or update) a field by position, use `_fp` (or `_fp!`). (`oc` is an object or a class.)

```
(define (_mp oc p) (vector-ref (caddr oc) p))
(define (_mp! oc p v) (vector-set! (caddr oc) p v))
(define (_fp o p) (vector-ref (car o) p))
(define (_fp! o p v) (vector-set! (car o) p v))
```

4.3 Method table operator

We define `_mteq?`, which takes an object or class `oc1` and an object or a class `oc2`. If they share the same method table, it returns true. Since the `cdr` of a class or object is its method table, it checks to see if the two arguments have the same method table.

```
(define (_mteq? oc1 oc2) (eq? (cdr oc1) (cdr oc2)))
```

We have to be sure that each class has a unique method table. We get that property, because each method vector gets a new `isa?` method, thus requiring a new method vector.

4.4 Making objects and accessing methods

We define `_n`, which given a class, creates a new object, and `_mv`, which given an object and a variable (symbol), accesses a method.

```
(define (_n c)
  (cons (make-vector (length (car c))) (cdr c)))

(define (_mv oc m)
  (_mp oc
    (let loop ([m* (cadr oc)] [pos 0])
      (if (eqv? (car m*) m)
        pos
        (loop (cdr m*) (+ pos 1))))))
```

We observe that accessing a method by its associated variable (a symbol) requires computing its position. When we use `_mv`, we say that we are accessing the method *externally*. These last three operators are different from the other six, since these three can be used anywhere, whereas the first six are restricted to class definitions. As such, we refer to the first six as *internal* and the remaining three as *external* interface operators.

We have now presented the nine interface operators. Next we present our object-oriented style and the example in this style. We then enforce some protocols on the style. Once we have the protocols in place, we then observe redundancy in the transformed program. Finally, we remove this redundancy with macro-generating macros.

`Exercise 2:` Using the definition of `e/o-procs` from Section 1.2, implement the procedures `even?` and `odd?`. Then implement `factorial` using this style. Each of the three procedures should take a single integer. ◇

5. OBJECT-ORIENTED STYLE

In this section we present the essence of an object-oriented style along with the test program and four classes written in this style. Upon conclusion of this section, the style should be clear and what remains has to do with improving the style's readability through protocols, method lifting strategies, and some macros, which allow the user to express the style more succinctly.

5.1 The style

Our object-oriented style is written in Scheme and uses the environment operator `append-env` (`enumerate-env` and `trim-env` are used in Section 8, only.), and our choice of representation for objects and classes. We liberally borrow terminology from Smalltalk, C++, and Java.

There are several facets of the style that we postpone until the classes and test programs are presented. Here, however, we give just a few fundamental aspects of the style. Some methods are not expressed as procedures built from `lambda` expressions, but those that are have `it`, which must be bound to an object or a class, as their first formal parameter. When `it` is bound to an object, we can access or set its fields. Every object of a given class uses the same position in its field vector for each field defined by the class. Thus, referencing and updating fields of objects of a given class is through constant positions within the field vector of `it`. To invoke a method in object-oriented style (It may also be just a procedure call.), first obtain the method through a constant position of a method vector, and then invoke it on some object or class and perhaps some additional arguments. Following the style means that if the method is from an object, then its first argument must be the object. If the method is from a class, then its first argument is either the class (rarely, but see the code of `isa?` below) or `it`. There are no restrictions on method bodies.

5.2 The example in our style

Below are four classes written in our object-oriented style. We refer to the class that we are currently defining as the *host* class. Each method of a host class is determined in one of two ways. Either it is the result of evaluating an expression (e.g., a `lambda` expression) or it is a method *contributed* (or *inherited*) from a single existing class, called its *super* class. Because we know that there is a one-to-one correspondence between the variables in the method environment of a class and the positions in the method vector of the class, we can think of the methods in the vector as if they had a name. For example, in the root class `<o>` below, we can associate `isa?` and `init` with the first two positions of its method vector.

```
(define <o>
  (list
    '()
    '(isa? init)
    (vector
      (lambda (it c)
        (_mteq? it c))
      (lambda (it . args)
        (void)))))

> <o>
(()
 (isa? init)
 #(#<isa?> #<init>))

(define <p>
  (list
    (_fx <o> '(x y))
    (_mx <o> '(move get-loc diag))
    (vector
      (lambda (it c)
        (or (_mteq? it c)
          ((_mp <o> 0) <o> c)))
      (lambda (it x^ y^)
        (_fp! it 0 x^)
        (_fp! it 1 y^)
        ((_mp <o> 1) it))
      (lambda (it dx dy)
        (_fp! it 0 (+ (_fp it 0) dx))
        (_fp! it 1 (+ (_fp it 1) dy)))
      (lambda (it)
        (list (_fp it 0) (_fp it 1)))
      (lambda (it a)
        ((_mp it 2) it a a)))))

> <p>
((x y)
 (isa? init move get-loc diag)
 #(#<isa?> #<init> #<move> #<get-loc> #<diag>))
```

In describing class `<p>` above, we say that the methods `isa?` and `init` are *replaced* (or *overridden*), since they replace already existing methods in (its super) class `<o>` associated with the same variable. We say that the methods `move`, `get-loc`, and `diag` are *fresh*.

The explicit list of variables in a call to `_fx` are the fresh field variables. They cannot contain duplicates and their order matters. The explicit list of variables in a call to `_mx` are the fresh method variables. They cannot contain duplicates, their order matters, and they are different from those in the super class. As the method vector is filled in, each method must fit into the right position. The replaced and contributed methods must be in the same positions as in their super class. The fresh methods must be placed after the replaced and contributed methods, and they must follow the order used in the call to `_mx`. There are no other constraints on how the method vector is built.

Consider this interactive session.

```
> (define p (_n <p>))
```

```
> ((_mp p 1) p 12 13)
> p
(#(12 13)
 (isa? init move get-loc diag)
 #(#<isa?> #<init> #<move> #<get-loc> #<diag>))
> ((_mv p 'move) p 14 15)
> (define map-nullary-method
    (lambda (o m*)
      (map (lambda (m) ((_mv o m) o)) m*)))
> (map-nullary-method p '(get-loc))
((26 28))
> ((_mp p 0) p <p>)
#t
```

The object `p` differs from the class `<p>` where the field vector and environment are stored. The field environment is `(x y)`, whereas the field vector is `#(12 13)`. We `move` `p`, which adds 14 to its `x` coordinate and 15 to its `y` coordinate, yielding its new location: `(26 28)`. We finish with a test of `isa?`. Next, we have the definition of the color point class.

```
(define <cp>
  (list
    (_fx <p> '(hue))
    (_mx <p> '(get-hue diag&set))
    (vector
      (lambda (it c)
        (or (_mteq? it c)
          ((_mp <p> 0) <p> c)))
      (lambda (it x^ y^ hue^)
        (_fp! it 2 hue^)
        ((_mp <p> 1) it x^ y^))
      (_mp <p> 2)
      (_mp <p> 3)
      (_mp <p> 4)
      (lambda (it) (_fp it 2))
      (lambda (it a)
        ((_mp it 4) it a)
        (_fp! it 2 a)))))

> <cp>
((x y hue)
 (isa? init move get-loc diag get-hue diag&set)
 #(#<isa?> #<init> ...))
```

We continue the interactive session.

```
> (define cp (_n <cp>))
> ((_mp cp 1) cp 16 17 7)
> cp
(#(16 17 7)
 (isa? init move get-loc diag get-hue diag&set)
 #(#<isa?> #<init> ...))

> ((_mv cp 'diag&set) cp 8)
> (map-nullary-method cp '(get-loc get-hue))
((24 25) 8)
> ((_mp cp 0) cp <p>)
#t
> ((_mp p 0) p <cp>)
#f
```

First, the color point `cp` has been painted 7. Then, its color has been changed to 8, which has been added to both its `x` and `y` coordinates. Then we have two `isa?` tests.

In `<o>`, we have no methods contributed from any super class, since `<o>` is the first one defined. In class `<p>` no method of its super class, `<o>`, has been contributed. In class `<cp>` the second, third, and fourth positions of `<p>` contribute a method. Thus we see that the same (`eq?`) method can be stored in more than one class. Finally, we define the stationary color point class `<scp>`.

```
(define <scp>
  (list
    (_fx <cp> '(y))
    (_mx <cp> '(show-y))
    (vector
      (lambda (it c)
        (or (_mteq? it c)
          ((_mp <cp> 0) <cp> c)))
      (lambda (it x^ y^ hue^)
        (_fp! it 3 ": Stuck: ")
        ((_mp <cp> 1) it x^ y^ hue^))
      (lambda (it x^ y^)
        ((_mp it 7) it))
      (_mp <cp> 3)
      (lambda (it a)
        (write (_fp it 2))
        ((_mp <cp> 4) it a))
      (_mp <cp> 5)
      (_mp <cp> 6)
      (lambda (it)
        (display (_fp it 3))))))

> <scp>
((x y hue y)
 (isa? init ... get-hue diag&set show-y)
 #(#<isa?> #<init> ...))
```

`Exercise 3:` Consider the results of this test.

```
(define test
  (lambda (c)
    (let ([p (_n <p>)]
          [cp (_n c)])
      ((_mp cp 1) cp 18 19 9)
      ((_mv cp 'diag&set) cp 10)
      (list
        (map-nullary-method cp '(get-loc get-hue))
        ((_mp cp 0) cp <p>)
        ((_mp p 0) p c)))))

> (test <scp>)
9: Stuck: (((18 19) 10) #t #f)
```

Why is a `9` displayed first and why is location `(18 19)` displayed instead of `(28 29)`? ◇

The internal interface operators are used primarily in extending environments and accessing (or updating) by position. When a class is passed to such an operator, it should be the

host's super class. We have no way of enforcing this restriction in this style, and furthermore, there are object-oriented languages where it is also not enforced.

A *chain* is a nonempty sequence of classes, linked by super classes, whose first element is a host class and whose last element is `<o>`. These classes form four chains. The shortest chain is of length one and starts at `<o>`, whereas the longest chain is of length four and starts at `<scp>`.

Although `_n` and `_mv` occur in the test only, it is still okay to use them within a method to create an object of *any* class or to externally access a method. One of the reasons for the confusion of the costs incurred by writing in object-oriented programming languages is that they do not *syntactically* distinguish between the two different ways of accessing a method: internally and externally. What is better, however, is to know that there is a search, possibly with a method-call cache or a hash table, whenever a method is accessed externally, as in `map-nullary-method`. For example, a different chain might have the method `move` associated with a position other than the second position. Clearly we cannot always rely on positions, but we can rely on `isa?`'s position being 0 and `init`'s position being 1.

We shouldn't rely on positions (except for `init`'s and `isa?`'s) in the test program above, because its code is not inside the class chain. Outside the class chain, we use a variable (symbol) to find its associated method.

We discover another bit of object-oriented style with the definitions of `<p>`, `<cp>`, and `<scp>`. Except in class `<o>`, the `isa?` method is replaced in each class definition; the first disjunct, `(_mteq? it c)`, is identical in each `isa?` method; and the second disjunct in `isa?` differs only in the reference to its host's super class. The `isa?` algorithm is a little tricky. The first call to `isa?` is different from all the others. In the first call to `isa?`, the value bound to `it` is an object. In the remaining calls, it is a class. So, the first call compares the method tables of an object and a class, but the other calls compare the method tables of two classes. In a sense, the remaining calls are just doing a kind of `member` search in a chain that starts at its host's super class.

What remains is to make the programs more eye-pleasing by introducing a small number of protocols, utilizing a lifting strategey, and presenting some macro-generating macros to manage redundancy. When we are done, we will have lost none of the power of Scheme and everything will be properly lexically scoped, so that although our tests rely on `define` (or `define-syntax`) for globals, they could as easily have relied on `let` (or `let-syntax`) for locals.

6. IMPOSING PROTOCOLS

There are three protocols that our object-oriented style uses. By enforcing these protocols, we approximate a conventional object-oriented language. First, we make the method bodies more readable by consistently using `super` to refer to the super class; second, we make the method bodies less conscious about method positions; and third, we do the same for field positions.

Henceforth, we focus exclusively on the code of the class definitions. Because of the confusion that is likely to arise by seeing lots of versions of all the classes, we confine our remaining transformations to class `<scp>`. We suggest revising `<o>`, `<p>`, and `<cp>` to verify your understanding.

`Exercise 4:` Each of the operators in the interface (such as `_fp` and `_mp`) takes an object or class as its first argument. Some methods have the property that they take an object or class as their first argument. Therefore, we can treat these operators as methods. Then it should also be possible to replace these methods. Think about these observations and implement a system where the interface operators are themselves methods. Also, consider representing the field environment as a *vector* of variables. (This exercise has been inspired by meta-object protocols [7].) ◇

`Exercise 5:` Use a single vector to represent classes by placing the method vector at index 0, the method environment at index 1, and each component of the field environment starting at index 2. Replace the use of `list` by `build-class` using its definition below,

```
(define build-class
  (lambda (f-env m-env m-vec)
    (list->vector
      (cons m-vec (cons m-env f-env)))))
```

and re-implement the nine interface operators to take advantage of this representation, which shrinks the cost of classes and objects with zero fields. ◇

6.1 Introducing `super`

Since `<scp>`'s super class `<cp>` appears many times in the preceding definition of `<scp>`, we can lift it out.

```
(define <scp>
  (let ([super <cp>])
    (list
      (_fx super '(y))
      (_mx super '(show-y))
      (vector
        (lambda (it c)
          (or (_mteq? it c)
              ((_mp super 0) super c)))
        (lambda (it x^ y^ hue^)
          (_fp! it 3 ": Stuck: ")
          ((_mp super 1) it x^ y^ hue^))
        (lambda (it x^ y^)
          ((_mp it 7) it))
        (_mp super 3)
        (lambda (it a)
          (write (_fp it 2))
          ((_mp super 4) it a))
        (_mp super 5)
        (_mp super 6)
        (lambda (it)
          (display (_fp it 3)))))))
```

This makes the definition of `isa?` more consistent: if `it` and the class are `_mteq?`, then `isa?` is true, otherwise try the `isa?` method of its host's super class, passing `super` along instead of `it`.

The decision to bind the lexical `super` to its host's super class makes it clear that `super` is always *static*. One of the confusing aspects of object-oriented programming, especially for neophytes, is whether one searches the chain of the class of `it` to find its `super`. This protocol clarifies that there is not even a search for `super`. The variable `super` however, must not be used in other ways. For example, binding it to another variable undermines some of the improvements in Section 8.2, and doing so leads inevitably to unexpected errors.

6.2 Position variables for methods

Next, we install the enumerated newly-created method environment and substitute the positions by their variables.

```
(define <scp>
  (let ([isa? 0]
        [init 1]
        [move 2]
        [get-loc 3]
        [diag 4]
        [get-hue 5]
        [diag&set 6]
        [show-y 7])
    (let ([super <cp>])
      (list
        (_fx super '(y))
        (_mx super '(show-y))
        (vector
          (lambda (it c)
            (or (_mteq? it c)
              ((_mp super isa?) super c)))
          (lambda (it x^ y^ hue^)
            (_fp! it 3 ": Stuck: ")
            ((_mp super init) it x^ y^ hue^))
          (lambda (it x^ y^)
            ((_mp it show-y) it))
          (_mp super get-loc)
          (lambda (it a)
            (write (_fp it 2))
            ((_mp super diag) it a))
          (_mp super get-hue)
          (_mp super diag&set)
          (lambda (it)
            (display (_fp it 3))))))))
```

6.3 Position variables for fields

We treat the field environment in a similar fashion. The field environment supports the *protected* variables. Since `y` in `<scp>` is the `y` at position 3 (not the `y` at position 1), we install the enumerated newly-created field environment with `let*`. This also says that any occurrences of `x` and `hue` are lexically visible here. The only way that one should be permitted to access `(_fp it 1)`, however, is by invoking a method defined in class `<p>`, which is rational behavior, or literally using the `1`, which is irrational behavior. Here is the revised `<scp>`,

```
(define <scp>
  (let* ([x 0] [y 1] [hue 2] [y 3])
    (let ([isa? 0] --- [show-y 7])
      (let ([super <cp>])
        (list
          (_fx super '(y))
          (_mx super '(show-y))
          (vector
            (lambda (it c)
              (or (_mteq? it c)
                ((_mp super isa?) super c)))
            (lambda (it x^ y^ hue^)
              (_fp! it y ": Stuck: ")
              ((_mp super init) it x^ y^ hue^))
            (lambda (it x^ y^)
              ((_mp it show-y) it))
            (_mp super get-loc)
            (lambda (it a)
              (write (_fp it hue))
              ((_mp super diag) it a))
            (_mp super get-hue)
            (_mp super diag&set)
            (lambda (it)
              (display (_fp it y)))))))))
```

where "`---`" indicates that there is some code that needs to be filled in. It should be obvious, but often just looking at the previous definition suffices.

One `let*` expression, which installs the field and method environments, would suffice. Even `super` could be included in the one `let*` expression. This explains why within a lexical scope no method variable (as a symbol) should be the same as a field variable (as a symbol) and furthermore, the symbol `super` should not be used as a method or field variable.

`Exercise 6:` Consider this definition of `<scp>`.

```
(define <scp>
  (let* ([x 0] [y 1] [hue 2] [y 3])
    (let ([isa? 0] --- [show-y 7])
      (let ([super <cp>])
        (list
          (_fx super '(y))
          (_mx super '(show-y))
          (_mxcct super
            `([isa? ,(lambda (it c) ---)]
              [init ,(lambda (it x^ y^ hue^) ---)]
              [move ,(lambda (it x^ y^) ---)]
              [diag ,(lambda (it a) ---)]
              [show-y ,(lambda (it) ---)])))))))
```

Implement `_mxcct`, which takes a class and a list of and method pairs and returns the appropriate method vector at class-construction time. ◇

We have reached the end of the discussion of object-oriented style. The style, especially with `_mxcct`, is good enough for most purposes, but we can improve its readability significantly.

7. LIFTING METHODS

We present three ways to lift methods. First, we lift the methods in a rather naive way; second, we use a scoping trick to obviate the need for worrying about contributed methods; and third, we bind each super method lexically.

7.1 Naive lifting

We can lift the methods out with a `let` expression, since the methods to be placed in the method vector are still lexically closed in the same environment. Furthermore, we can use the variable associated with the method as the binding variable within the `let`. The order of the bindings in the `let` expression *does not* matter, but the order of the methods in the vector *does*.

```
(define <scp>
  (let* ([x 0] [y 1] [hue 2] [y 3])
    (let ([isa? 0] --- [show-y 7])
      (let ([super <cp>])
        (let ([isa? (lambda (it c) ---)]
              [init (lambda (it x^ y^ hue^) ---)]
              [move (lambda (it x^ y^) ---)]
              [get-loc (_mp super get-loc)]
              [diag (lambda (it a) ---)]
              [get-hue (_mp super get-hue)]
              [diag&set (_mp super diag&set)]
              [show-y (lambda (it) ---)])
          (list
            (_fx super '(y))
            (_mx super '(show-y))
            (vector isa? --- show-y)))))))
```

7.2 Triply-nested `let`

Next, we present a scoping trick to create a method vector. It allows us to use scoping alone to determine the replaced and contributed methods.

```
(define <scp>
  (let* ([x 0] [y 1] [hue 2] [y 3])
    (let ([isa? 0] --- [show-y 7])
      (let ([super <cp>])
        (let ([g0 (lambda (it c) ---)]
              [g1 (lambda (it x^ y^ hue^) ---)]
              [g2 (lambda (it x^ y^) ---)]
              [g3 (lambda (it a) ---)]
              [g4 (lambda (it) ---)])
          (let ([isa? (_mp super isa?)]
                [init (_mp super init)]
                [move (_mp super move)]
                [get-loc (_mp super get-loc)]
                [diag (_mp super diag)]
                [get-hue (_mp super get-hue)]
                [diag&set (_mp super diag&set)])
            (let ([isa? g0]
                  [init g1]
                  [move g2]
                  [diag g3]
                  [show-y g4])
              (list
                (_fx super '(y))
                (_mx super '(show-y))
                (vector isa? --- show-y)))))))))
```

We know that we can scramble the order of the bindings in the `let` expression without affecting its semantics. This version uses as many temporaries `g0`–`g4` as there are new host (i.e., replaced and fresh) methods. The code still closes the method expressions in the position environments. Then it binds *all* the super methods, however, any that are being replaced get rebound in the last `let` of the triply-nested `let`. If a compiler could determine that `_mp` is effect free, no code should be generated for the binding of the super `isa?`, `init`, `move`, and `diag` methods, since they are being lexically shadowed. Thus, the same variable, for example `isa?`, changes from being bound to a position, to being bound to a super method, then to being bound to a replaced method.

7.3 Quadruply-nested `let`

We can include an additional outer `let` layer using the following strategy. Since we know the super class, we bind each super method to a super temporary, `h0`–`h6`. Then we substitute each super method access (`_mp super ---`) within the body of this new `let` by its super temporary.

```
(define <scp>
  (let ([super <cp>])
    (let* ([x 0] [y 1] [hue 2] [y 3])
      (let ([isa? 0] --- [show-y 7])
        (let ([h0 (_mp super isa?)]
              ---
              [h6 (_mp super diag&set)])
          (let ([g0 (lambda (it c)
                      (or (_mteq? it c)
                        (h0 super c)))]
                [g1 (lambda (it x^ y^ hue^)
                      (_fp! it y ": Stuck: ")
                      (h1 it x^ y^ hue^))]
                [g2 (lambda (it x^ y^)
                      ((_mp it show-y) it))]
                [g3 (lambda (it a)
                      (write (_fp it hue))
                      (h3 it a))]
                [g4 (lambda (it)
                      (display (_fp it y)))])
            (let ([isa? h0]
                  ---
                  [diag&set h6])
              (let ([isa? g0]
                    [init g1]
                    [move g2]
                    [diag g3]
                    [show-y g4])
                (list
                  (_fx super '(y))
                  (_mx super '(show-y))
                  (vector isa? --- show-y)))))))))))
```

We have chosen this unorthodox approach because we want to point out the extent to which scope can be used to solve problems. We could have used the naively lifted version of `<scp>` instead in `build-shadow` below, but then we would have needed an additional position environment operator. Also, with the binding of the super methods, it becomes even more obvious that super method calls are static.

Exercise 7: Our characterization of field variables yields protected variables. We can make some of them *private* instead of protected. Assume that `unique` is a variable that will never be used as a field or method variable. When we build, but *not* install, the host's field environment, we replace each private variable by `unique`. Thus, the only way that the field can be accessed is through a method in its host. Using `unique`, determine the field environment of classes `<cp>` and `<scp>` so that `hue` of `<cp>` is private. Since `get-hue` gets contributed to any class that has `<cp>` in its super class chain, we can revise `diag` of `<scp>` to use it instead of `hue`. ◇

Exercise 8: Our characterization of method variables yields protected variables. We can make some of them private instead of protected. We associate with each method variable a boolean indicating whether (`#f`) or not (`#t`) a variable is private. Then accessing using `_mv` is permissible if the associated boolean is `#t`. But, `_mp` is where the problem gets interesting. If we limit the use of `super` to methods that are being replaced with the same variable, then even if we make the variable private in the super class, we should still be able to access it. But, we should not be able to access a private method variable in the super class with an object. When we install the method environment in the host, we use different unique variables for each method that has been designated private in the super class. If we installed with `let*`, we could use one unique variable as in the preceding exercise. Make `move` private in class `<p>` by revising the class chain. ◇

8. SIMPLIFYING THE SYNTAX

We now recognize four improvements that we can make to the readability of the code. First, we observe that the `isa?` method in each class other than `<o>` looks the same. Second, we do not need to worry about which methods are being contributed. If they come from the super class and are not being replaced, then they are being contributed. Third, we limit internal method access to calls that appear syntactically like procedure calls. Fourth, we make field reference appear like variable reference and field update appear like `set!`. The second version of `extender` combined with `build-shadow`, presented below, is our eventual goal. To reach this goal, we need the notion of a *shadow*, which we now describe.

8.1 Defining a shadow per class

A *shadow* is a macro that manages the *static* information of a class. That includes the field and method environments. The *behavior* of a class is the method vector, which we can mostly ignore. We present a simple way with one complex macro to capture the protocols of object-oriented style.

Each shadow can be used in three ways. First, it might be used as a super shadow in the definition of another shadow, just as a class might be used as a super class. This leads to the higher-order macro `extend-shadow` that takes the super shadow as a parameter. Second, it might be used for accessing a method externally at macro-expansion time. This leads to the higher-order macro `invoke`, which we describe in Section 9. Third, it might be used to build a class with a super class. The super class is needed, of course, for accessing the contributed methods. This leads to the higher-order macro `create-class` that also takes the host shadow as a parameter. So the shadow macro contains a dispatch to select one of these three tasks. Before we analyze them, let's look at how they would be used to define `<scp>`, assuming that shadow `<<o>>` and its associated class `<o>` exist.

```
(define-syntax <<p>> (extend-shadow <<o>> ---))
(define <p> (create-class <<p>> <o>))
(define-syntax <<cp>> (extend-shadow <<p>> ---))
(define <cp> (create-class <<cp>> <p>))
```

```
(define-syntax <<scp>>
  (extend-shadow <<cp>> (y)
    ([init
       (lambda (it x^ y^ hue^)
         (_fp! it y ": Stuck: ")
         ((_mp super init) it x^ y^ hue^))]
     [move
       (lambda (it x^ y^)
         ((_mp it show-y) it))]
     [diag
       (lambda (it a)
         (write (_fp it hue))
         ((_mp super diag) it a))]
     [show-y
       (lambda (it)
         (display (_fp it y)))])))

(define <scp> (create-class <<scp>> <cp>))
```

Exercise 9: Complete `<<p>>` and `<<cp>>`. ◇

The macro `extend-shadow` below expands into an invocation of the macro `sup-shadow`. The `extend-shadow`'s first operand is a (super) shadow. Its second operand is a list of fresh (host) field variables that we are making available. This means, for example, that the shadow `<<scp>>` has one more item in its field environment than those of its super shadow, `<<cp>>`. Its last operand is a list of "`let`" pairs that define the new host methods. Here is where we take advantage of the fixed structure of the `isa?` method by automatically including it in every shadow, except `<<o>>`. The expansion of `sup-shadow` generated by the expansion of `extend-shadow` takes three operands. The first of these items "`_`" is the syntactic context that dictates which macro expansion a variable comes from. By passing it along, we can use it to control variable hygiene. The remaining operands are the fresh field variables and the new host method "`let`" pairs of the host class, with the addition of the `isa?` method "`let`" pair.

```
(define-syntax extend-shadow
  (lambda (x)
    (syntax-case x ()
      [(_ sup-shadow (f-var ...) ([m-var e] ...))
       (with-implicit (_ super isa?)
         #'(sup-shadow _ (f-var ...)
             ([isa? (lambda (it c)
                      (or (_mteq? it c)
                        ((_mp super 0) super c)))]
              [m-var e] ...)))])))
```

The definition of `extender` in Figure 1 requires that all occurrences of `super` refer to the same lexical variable. We do this using `with-implicit` (Figure 1) by turning the symbol `'super` into the variable `super`. Any macro system that supports `syntax-case` should support `with-implicit`. Without `with-implicit`, variable hygiene would cause the variable `super`, which is a formal parameter of the `lambda` expression, to be renamed to some fresh variable, causing occurrences of `super` in the body to be treated as free. (See Dybvig [4].)

The macro `create-class` takes a host shadow of some class c (to be defined) and a super class of c.

```
(define-syntax create-class
  (syntax-rules ()
    [(_ host-shadow super-class)
     ((host-shadow) super-class)]))
```

With these two items, it builds c. The macro call generated by a call to `create-class` takes zero operands. This zero-operand macro call expands into an expression that evaluates to a procedure of one argument. In `build-shadow` (Figure 1), the clause can be recognized by the simple pattern `(__)`. The procedure's argument is either `#f` or some super class. If it is `#f`, it means we are defining `<o>` and it is ignored.

The `build-<<o>>` macro defers to `build-shadow`, but it passes the empty field and method environments as its "super" environments. The third empty list is passed because our class `<o>` has no fields. The fourth list is a list of (fresh) methods for `<o>`, including a temporary for each. Recall in Section 7.2 where we needed the temporaries, `g0`–`g4`. Each second item in the "`let`" triple is its associated temporary.

```
(define-syntax build-<<o>>
  (lambda (x)
    (syntax-case x ()
      [(_ ([m e] ...))
       (with-syntax
         ([(g ...)
           (generate-temporaries #'(m ...))])
         #'(build-shadow _ () () ()
             ([m g e] ...)))])))
```

Then, we can use the definition of the shadow `<<o>>` to define the class `<o>`.

```
(define-syntax <<o>>
  (build-<<o>>
    ([isa?
       (lambda (it c)
         (_mteq? it c))]
     [init
       (lambda (it . args)
         (void))])))

(define <o> (create-class <<o>> #f))
```

Now we come to the heart of the matter, `build-shadow` (Figure 1), which creates the shadow macro for a class. The input is a list of field and method variables for the super shadow followed by the field variables and method "`let`" triples for the host shadow. The macro first combines the field and method variables of the super and the host shadows, translating from syntax to datum and back again. The `build-shadow` macro then returns the shadow macro, `#'(lambda (xx) ...)`. As described above, this macro dispatches either to create a class (the clause with `(__)` pattern), to access a method (the clause with `(__ an-m-var oc)` pattern), or to create a new shadow with this shadow as its super. (The `(... ...)` is a nested ellipsis. As the syntactic levels get more deeply nested, so do the ellipses.)

In the case of creating a class (See `extender` in Figure 1.), the macro returns an expression that evaluates to a procedure expecting the super class (or `#f`), which is bound to the variable `super` in the lexical scope surrounding the method bodies. The body of the procedure returns code that includes the invocation of `list` to build the class with the quadruply-nested `let` expression.

In the case of accessing a method (See the second clause of the shadow returned from `build-shadow`.), the shadow uses the method variable and all the method variables and their positions of its shadow to find the associated position of the method variable. This is used for external method accessing, which is described in Section 9.

In the case of creating a new shadow, temporaries are generated for the methods, and then `build-shadow` is invoked for the new host, with this shadow as its super. For example, when we invoke `extend-shadow` with `<<cp>>` and the body of the *future* `<<scp>>`, this invokes the third clause in the `<<cp>>` shadow, thus calling `build-shadow` with the super field and method variables from `<<cp>>` and host information from the body of the future `<<scp>>`. The result is the new shadow macro `<<scp>>`. Further, when we call `(create-class <<scp>> <cp>)`, the first clause in the shadow macro `<<scp>>` is called. Its expansion returns an expression that evaluates to a procedure expecting a super class. The procedure is immediately applied to `<cp>`. The result is the list representation for the new version of class `<scp>`.

Although we have implied that each class is created as soon as we have defined its shadow, that ordering is not required. Instead, we only need the *shadow to be defined* before creating its associated class. Thus, we could create a bunch of shadows and then create a bunch of classes that were built from these shadows.

8.2 Simplifying method calls and fields

Now we redefine `extender` (Figure 2) so that internal method calls look like regular procedure calls, and field variables look like regular lexical variables. Thus, occurrences of `((_mp o m) o arg ...)` can be rewritten as `(m o arg ...)`. Also occurrences of `(h`k `it arg ...)`, where `h`k is a lexically scoped super method variable for the super method `m`, can be rewritten as `(m super arg ...)`. Similarly, occurrences of `(_fp it f)` can be rewritten as the variable `f`, and occurrences of `(_fp! it f v)` can be rewritten as `(set! f v)`. (See Section 2 for examples.)

```
(define-syntax with-implicit
  (syntax-rules ()
    [(_ (ctx id ...) body0 body1 ...)
     (with-syntax ([id (datum->syntax-object #'ctx 'id)] ...) body0 body1 ...)]))

(define-syntax extender
  (lambda (x)
    (syntax-case x ()
      [(_ ctx ([s k] ...) (all-f ...) ([f j] ...) ([m i] ...) ([m-var g e] ...))
       (with-syntax ([(h ...) (generate-temporaries #'(s ...))])
         (with-implicit (ctx super)
           #'(let ([f j] ...)
               (let ([m i] ...)
                 (lambda (super)
                   (let ([h (_mp super k)] ...)
                     (let ([g e] ...)
                       (let ([s h] ...)
                         (let ([m-var g] ...)
                           (list '(all-f ...) '(m ...) (vector m ...)))))))))))]))

(define-syntax assv-macro
  (lambda (x)
    (syntax-case x ()
      [(_ i ([k0 h0] [k1 h1] ...))
       (if (eqv? (syntax-object->datum #'k0) (syntax-object->datum #'i)) #'h0
           #'(assv-macro i ([k1 h1] ...)))])))

(define-syntax build-shadow
  (lambda (x)
    (syntax-case x ()
      [(_ ctx sup-f sup-m (f-var ...) ([m-var g e] ...))
       (let ([sup-f (syntax-object->datum #'sup-f)]
             [sup-m (syntax-object->datum #'sup-m)]
             [f-vars (syntax-object->datum #'(f-var ...))]
             [m-vars (syntax-object->datum #'(m-var ...))])
         (let ([f (append-env sup-f f-vars)]
               [m (append-env sup-m (fresh-m-vars m-vars sup-m))])
           (with-syntax
               ([([s k] ...) (datum->syntax-object #'ctx (enumerate-env sup-m))]
                [([m i] ...) (datum->syntax-object #'ctx (enumerate-env m))]
                [([f j] ...) (datum->syntax-object #'ctx (trim-env (enumerate-env f)))]
                [(all-f ...) (datum->syntax-object #'ctx f)])
             #'(lambda (xx)
                 (syntax-case xx ()
                   [(__)
                    #'(extender ctx ([s k] ...) (all-f ...) ([f j] ...) ([m i] ...) ([m-var g e] ...))]
                   [(__ an-m-var oc) #'(_mp oc (assv-macro an-m-var ([m i] ...)))]
                   [(__ ctx (f-var^ (... ...)) ([m-var^ e^] (... ...)))
                    (with-syntax ([(g^ (... ...)) (generate-temporaries #'(m-var^ (... ...)))])
                      #'(build-shadow ctx (all-f ...) (m ...)
                          (f-var^ (... ...))
                          ([m-var^ g^ e^] (... ...))))]))))))]))

(define fresh-m-vars
  (lambda (m-vars sup-m-vars)
    (cond
      [(null? m-vars) '()]
      [(memv (car m-vars) sup-m-vars) (fresh-m-vars (cdr m-vars) sup-m-vars)]
      [else (cons (car m-vars) (fresh-m-vars (cdr m-vars) sup-m-vars))])))
```

Figure 1: The `build-shadow` macro using `extender`

```
(define-syntax if-shadowed
  (lambda (x)
    (syntax-case x ()
      [(_ id ctx conseq altern)
       (if (not (free-identifier=? #'id
                  (datum->syntax-object #'ctx
                    (syntax-object->datum #'id))))
         #'conseq
         #'altern)])))

(define-syntax field-var
  (lambda (x)
    (syntax-case x ()
      [(_ ctx id it j)
       #'(identifier-syntax
           [var (if-shadowed id ctx id (_fp it j))]
           [(set! var val) (if-shadowed id ctx (set! id val) (_fp! it j val))])])))

(define-syntax method-var
  (lambda (x)
    (syntax-case x ()
      [(_ ctx mapping m super it i)
       #'(lambda (x)
           (syntax-case x (super)
             [(m_ super arg (... ...))
              #'(if-shadowed m ctx (m super arg (... ...)) ((assv-macro i mapping) it arg (... ...)))]
             [(m_ oc arg (... ...))
              #'(if-shadowed m ctx (m o arg (... ...)) (let ([o^ o]) ((_mp o^ i) o^ arg (... ...))))]
             [(m_)
              #'(if-shadowed m ctx (m) (error 'method "Cannot take zero arguments:" m))]
             [m_ (identifier? #'m_)
              #'(if-shadowed m ctx m (error 'method "Cannot be a symbol:" m))]))])))

(define-syntax extender
  (lambda (syn)
    (syntax-case syn ()
      [(_ ctx ([s k] ...) (all-f ...) ([f j] ...) ([m i] ...) ([m-var g e] ...))
       (with-syntax ([(h ...) (generate-temporaries #'(s ...))])
         (with-implicit (ctx super method)
           #'(lambda (super)
               (let ([h (_mp super k)] ...)
                 (let-syntax
                   ([transf-body
                      (lambda (xx)
                        (syntax-case xx ()
                          [(_ __ ctx body0 body1 (... ...))
                           (with-implicit (__ it super set! f ... m ...)
                             #'(let-syntax ([f (field-var ctx f it j)] ...)
                                 (let-syntax ([m (method-var ctx ([k h] ...) m super it i)] ...)
                                   body0 body1 (... ...))))]))])
                   (let-syntax
                     ([method
                        (lambda (xx)
                          (syntax-case xx ()
                            [(__ params body0 body1 (... ...))
                             (with-implicit (__ it)
                               #'(lambda (it . params)
                                   (transf-body __ ctx body0 body1 (... ...))))]))])
                     (let ([g e] ...)
                       (let ([s h] ...)
                         (let ([m-var g] ...)
                           (list '(all-f ...) '(m ...) (vector m ...)))))))))))])))
```

Figure 2: The `extender` macro for method calls and fields

This `extender` includes the definition of the local macro, `method`, which makes anonymous methods within an `extend-shadow` just as `lambda` makes anonymous procedures. The difference is that with `method` it assumes implicitly that the first argument is bound to the variable `it`. Thus, the number of formal parameters in a `method` expression is one fewer than those of the equivalent `lambda` expression.

The local macro `method` looks more complicated than it is. Basically, it is the same as `lambda` but includes `it` as its first formal parameter. Because of variable hygiene, however, we have to make the macro system believe that `it` had been one of the operands of `method`. The "`__`" syntactic context indicates exactly which macro call to associate with the new variable. Thus, `it` is now ready to be treated as a piece of syntax. We place it as the first formal parameter of the resulting `lambda` expression. This use of `with-implicit` forces all free occurrences of `it` in `body0 body1 ...` to be treated as bound in the `lambda` expression.

Next, we focus on `(let-syntax ([m ...])`. Each `m` call generates one of two calls. If it is a super call, we generate a procedure call using one of the procedures bound to, for example, the `h0`–`h6` temporaries. Otherwise we generate the object method call. In the second variant, we use a `let` expression just in case the argument is other than a variable.

Also, we improve the syntax of field access and update. Consider the line that starts out `(let-syntax ([f ...])`. Where `j` is `f`'s position, then each `f` is to be expanded to `(_fp it j)`, and each `(set! f v)` is to be expanded to `(_fp! it j v)`. In the first `extender` we constructed the subset of the field environment with `trim-env`. We need this particular subset of the field environment, since we care only about protected positions.

By including the `super` and the `f ... m ...` in the exact match list, we know that we only concern ourselves with the specific field and method variables we care about. All the other cases treat `f ...` and `m ...` as lexical variables. The variable `super` is now treated as both a regular lexical variable and as a target of comparison (See Section 6.1.). Furthermore, we cannot forget to capture `(f ... m ...)` using the "`__`" passed in through `transf-body`.

These abbreviations have a real benefit. Not only do we get to use the familiar syntax, but we also get to remove the two `let`s that had been used to install the method and trimmed field environments of the first `extender`. Why? We can do this because we are inserting the actual positions in the expanded code.

`Exercise 10:` Now that we no longer need the run-time field environment, we observe that the only place it is used is in the definition of `_n`, which we redefine.

```
(define (_n c)
  (cons (make-vector (car c)) (cdr c)))
```

This definition clarifies that we need only store the field environment's *length*, which can be determined at macro-expansion time. Change `extender` appropriately. ◇

8.3 Expanding `create-class`

Below is the expansion of `(create-class <<scp>> <cp>)`, where we manually put back the `let`s and `or`, and, where we use "`---`" as above. It differs from the definition that appears in Section 7.3 in four ways. First, the field and method environments have been built at macro-expansion time, thus obviating the need for `_fx` and `_mx`; second, the installed `let*` and installed `let` have vanished; third, there is a `let` binding that refers to `it`, which vanishes at compile time; and fourth, `(_mp super isa?)` has not been expanded to `h0`, since it takes `super`, not `it`, as its implied argument.

```
(let ([super <cp>])
  (let ([h0 (_mp super 0)]
        ---
        [h6 (_mp super 6)])
    (let ([g0 (lambda (it c)
                (or (_mteq? it c)
                  ((_mp super 0) super c)))]
          [g1 (lambda (it x^ y^ hue^)
                (_fp! it 3 ": Stuck: ")
                (h1 it x^ y^ hue^))]
          [g2 (lambda (it x^ y^)
                (let ([o^ it])
                  ((_mp o^ 7) o^)))]
          [g3 (lambda (it a)
                (write (_fp it 2))
                (h4 it a))]
          [g4 (lambda (it)
                (display (_fp it 3)))])
      (let ([isa? h0]
            ---
            [diag&set h6])
        (let ([isa? g0]
              [init g1]
              [move g2]
              [diag g3]
              [show-y g4])
          (list
            '(x y hue y)
            '(isa? --- show-y)
            (vector isa? --- show-y)))))))
```

`Exercise 11:` We can extend Exercise 2 to include adding new host methods. We can get recursion by using zero fields and forcing all but the first method access to be internal. Implement `factorial`, `even?`, and `odd?` as follows. Build `<factorial>` with `fact` as its only fresh method. Next, implement the two mutually-recursive methods `iseven` and `isodd` by defining a three element chain: `<o>`, `<even?>`, and `<odd?>`. The class `<even?>` contains the method `iseven` and the class `<odd?>` contains the method `isodd`. First solve it for a chain of `<o>` and `<even?/odd?>`. ◇

`Exercise 12:` Design a syntax for a call like we use in the super call of `isa?`, so that it expands to `h0` instead of `(_mp super 0)`. ◇

`Exercise 13:` Implememnt the macro-expansion-time analog of `isa?`, which expands to a boolean constant. ◇

8.4 Lexical scope versus protected scope

In this section we analyze how the new `extender` interacts with lexical scope. This semantics differs from that of Section 8.1. There, we interposed the protected scope by installing artificial position environments, which should not necessarily shadow lexical variables. (This use of "shadow" should not be confused with the use in Section 8.1.)

We have to make decisions about what variables lexically shadow what other variables. In `<<escp>>` below, what values of `hue` would we expect to be displayed if we passed `(create-class <<escp>> <scp>)` to `test`? We would hope that any introduced lexical scope in the method such as the `(let ([hue "inside "])` or the formal parameter of `init` would shadow the field variable, and indeed it does. Even the one `hue` bound *outside* the method expression of `show-y` displays the value of the lexical variable `hue` instead of the value of the protected field variable.

```
(define-syntax <<escp>>
  (extend-shadow <<scp>> ()
    ([init
       (method (x^ y^ hue)
         (display hue)
         (init super x^ y^ hue))]
     [show-y
       (let ([hue "outside "]
             [diag* (lambda (x y)
                      (display "moving "))])
         (method ()
           (display hue)
           (diag* 5 5)
           (let ([hue "inside "]
                 [diag (lambda (n self)
                         (diag self n))])
             (display hue)
             (diag 5 it))))])))
```

The expression `(diag 5 it)` is lexically scoped within `(let ([diag ...])`, but the variable `diag` in the expression `(diag self n)` does indeed refer to the method. If we were to run our test program using `<<escp>>`, it would loop indefinitely, because of the mutually recursive tail calls from `diag` (contributed from `<scp>`) to `move` (contributed from `<scp>`), then to the host method `show-y`, and then back to `diag`. This loop would happen even if we were to rewrite `self` with another randomly chosen variable `super`, since the expansion of the `diag` *procedure* would then have been

```
(lambda (n super_1)
  (let ([o^ super_1])
    ((_mp o^ 3) o^ n)))
```

But, if we were to α-substitute `diag*` by `diag`, then `(test)` would terminate, after displaying `moving`.

Any free variables outside a method expression are lexically scoped. This decision is quite arbitrary, but any reasonable characterization of which variables shadow which other variables can be implemented using `syntax-case` (See Dybvig [4].). We believe that our structuring of the scopes is reasonable, since otherwise the programmer would have to know all the protected variables in the host's chain. This is what we need `if-shadowed` for (Figure 2). It chooses the third operand if a variable inside a method expression is shadowed by a lexical variable bound in the scope outside of the method expression but within an `extend-shadow` expression. Our characterization is a two-edged sword, however. This example loops and then fails to loop when a lexical variable bound outside a method expression but within an `extend-shadow` expression is inadvertently α-substituted by a protected variable. A general solution that circumvents this problem is to require that when in doubt, field and method variables should be private (See Exercises 7 and 8.).

The example below shows that we have lost no lexical scope.

```
(define <escp>-maker
  (lambda (x)
    (let-syntax
      ([<<escp>>
         (extend-shadow <<scp>> ()
           ([e (begin
                 (write x)
                 (let ([y 1])
                   (method (q r . args)
                     (+ x y q r (car args)))))])))])
      (lambda (s)
        (create-class <<escp>> s)))))

> (let ([escp (_n ((<escp>-maker 1) <scp>))])
    ((_mp escp 1) escp 10 20 7)
    ((_mv escp 'e) escp 1 1 1))
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```

First the digit `1` appears, since `x` is a free variable. Even though `x` is a protected variable within the method expression, the occurrence of `x` in `(write x)` is free within the `extend-shadow` expression. That would be true even if we introduced a fresh field or method variable, `x`. The protected variable `x` has the value `10` and it shadows the `x` outside the `extend-shadow` expression. The `14` is not greater than `20`, since `y` is scoped between a method expression and an `extend-shadow` expression. But, if we were to α-substitute `x` by `z`, the value would be `5`. If we then rewrite `[y 1]` as `[t 1]`, the result would be `24`, since now `y` would be protected instead of lexical and would have the value `20`.

`Exercise 14:` Hand-build `<<o>>` and `<o>` without using `build-<<o>>`, `build-shadow`, or `create-class`. We know that when we create class `<o>`, we do it by passing in `#f`. Therefore, we can do some of the expansion ourselves. The `#f` gets bound to `super`, but we know that `<<o>>` has no super methods, so only the second and fourth parts of the quadruply-nested `let` are used. Then it becomes obvious that we can go from this doubly-nested to a single `let`. $\diamond$

`Exercise 15:` Implement the following variant on the scope rules. Instead of allowing protected variables to shadow some lexical variables, just have the host's protected variables as possibly shadowing some lexical variables. Next, implement scope rules to make lexical variables shadow protected variables. $\diamond$

Exercise 16: Add a method table that uses `let*` when installing its method environment, and add an environment and associated vector for fields that uses `let` when installing its field environment. Thus each class has an additional field environment and method table, and each object has an additional field vector. ◇

9. MORE EXTERNAL OPERATORS

We have three more external operators to define. The first `new` is a more general variant of `_n`. Each of the other two, `mbv` and `invoke`, avoid computing a method variable (symbol) when they are used to externally access a method.

With `new` below, we invoke the method `init`, which takes any number of operands.

```
(define-syntax new
  (syntax-rules ()
    [(_ c arg ...)
     (let ([o (_n c)])
       ((_mp o 1) o arg ...)
       o)]))
```

There are two aspects of `new` that deserve mention. First, `new` takes at least one argument. That one argument should be a class. Second, we know that we are going to invoke the method `init`, whose position is `1`.

We might want operators that allow us to avoid computing a method variable (symbol) when we are externally accessing it. We can do this in two ways. One way is by accessing the method using a quoted variable with `mbv` (invoke method by variable) below. This, however, still requires a run-time search to access the method.

```
(define-syntax mbv
  (syntax-rules ()
    [(_ m oc arg ...)
     (let ([oc^ oc])
       ((_mv oc^ 'm) oc^ arg ...))]))
```

Alternatively, we can invoke a method whose position has been determined at macro-expansion time with `invoke` below. This is where we use the clause in `build-shadow` whose pattern is `(__ an-m-var oc)`. But, we need to refer to some shadow that contains the *appropriate* method variable `m`.

```
(define-syntax invoke
  (syntax-rules ()
    [(_ shadow m oc arg ...)
     (let ([oc^ oc])
       ((shadow m oc^) oc^ arg ...))]))
```

We use `let` here to avoid evaluating `oc` twice. We cannot always use `invoke`. Only rarely is it necessary to use `mbv`, and it is even less likely that one would need the full unbridled power of `_mv`. Of course, this last claim is subject to closer scrutiny, since the message-passing model of object-oriented programming relies heavily on messages being symbols

Consider `test-<scp>` below.

```
(define test-<scp>
  (lambda ()
    (let ([p (new <p> 1 2)]
          [scp (new <scp> 18 19 9)])
      (invoke <<scp>> diag&set scp 10)
      (list
        (list
          (invoke <<scp>> get-loc scp)
          (invoke <<cp>> get-hue scp))
        (isa? scp <p>)
        (isa? p <scp>)))))

(define isa?
  (lambda (it c)
    ((_mp it 0) it c)))
```

We define a useful predicate, `isa?`, and we restrict external method access to be through the use of `invoke` or `mbv`. Hence, `map-nullary-method` can no longer be used. Why?

Exercise 17: Why is it okay to use `<<cp>>` in `(invoke <<cp>> get-hue scp)` instead of `<<scp>>` even though `scp` is of class `<scp>`? What would happen if we revised it with `<<p>>`? ◇

10. CONCLUSIONS

Our goal has been to demonstrate that by thinking about the actual structure of the method and field environments and their associated vectors, we can better appreciate the subtlety of the semantics of object-oriented programming. We have done this by first developing an object-oriented style, then protocols, a lifting strategy, and finally `extend-shadow` and `create-class` with some supporting macros. Because enough of the system has been built with macros, all the shadows can be built at macro-expansion time.

Let us revisit our goals. Most conventional languages use implementation technology that makes writing recursive programs a risky enterprise. Now, object-oriented programming has inadvertently made recursion the natural way to write programs. But still the implementation technology does not yet allow the recursion to be exploited, since most (object-oriented) languages do not support tail-call optimization.[2] Also, a goal has been to clarify just how different super method invocation is from object method invocation. Knowing that `super` is static should make the distinction obvious. Furthermore, the quadruply-nested `let` of Section 7.3 treats super calls as regular procedure calls, where the super procedure is bound to a lexical variable.

The `extend-shadow` macro is merely a compiler for the language supported in the definition of `<<scp>>` and `<scp>` of Section 2. The compiler, among other activities, substitutes *all* the position variables by their corresponding positions. And, as we demonstrate in Section 8.3, this compiler produces code virtually the same as our examples of object-oriented style in Section 5.2.

[2]The designers of C# claim, however, to support tail-call optimization, at least in spirit.

We have been able to preserve the property that when the scope of a variable is in question within an `extend-shadow` expression, lexical scope shadows the protected scope of field and method variables. We show in Section 8.4 that `extend-shadow` and any method within `extend-shadow` can be wrapped in lexical scope, so no scope whatsoever has been lost. Also, the body of a method, itself, can evaluate to a procedure, which in turn can be invoked in object-oriented style. A new host method passed to `extend-shadow` needn't be introduced with a `method` expression (or `lambda` expression). It can be any legal expression. Furthermore, if the expression's value happens to be a procedure of at least one argument, even if it is not wrapped within the `method` keyword, it can be invoked in object-oriented style. This is a feature, however, that should be used with extreme caution, since then it could be a variable bound to a reified continuation or it could be a procedure that reveals the underlying representation of objects and classes.

This development says something about macros, in general. Macros have come a long way from the early days of Lisp. Now, with hygiene, `with-syntax`, `syntax-case`, etc., we see that macros are powerful enough to write sophisticated compilers. More importantly, the compiler can be written so that the expressions are not explicitly traversed by the macro writer's code, improving its portability.

Our analogy with continuation-pssing style is not fully developed. Object-oriented and continuation-passing styles get their extra power with an extra argument. That power comes from a careful harnessing of different dynamic aspects of computation. Our future plans include formally characterizing our object-oriented style. There is clearly a style here, but we have so far just been able to describe it informally. A concern with formalizing our style is that the subtle issues of wiring the lexical scope and making the encoding robust enough to be an embedding might be overlooked. Also, we hope to have transformers to object-oriented style just as there are transformers to continuation-passing style.

From the beginning, our plan has been the transmutation of symbols into variables. This effort has taken longer than one would have expected, given the relative simplicity of its solution. Nevertheless, this is just our first result of this kind where symbols are not accepted as the natural currency of computation. A symbol, of course, is a run-time value. Now that our macro systems have become so sophisticated, we have an opportunity to think much harder about processing programs well before they run and turning other classes of symbols into variables.

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